



Cellular Automata Models of Pedestrian Dynamics

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Overview

Pedestrian dynamics

- interesting collective effects
- simple model ?
- learning from nature?
- similarities with ant trails

unified description of pedestrian dynamics
and ant trails!

Ant trails vs. human trails

ant trail



human trail



Pedestrian Dynamics

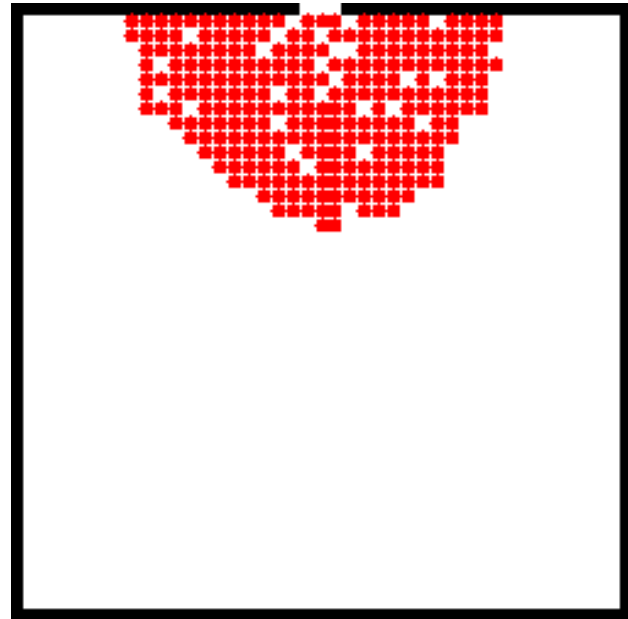
More **complex** than highway traffic

- motion is **2-dimensional**
- **counterflow** important
- interaction “**longer-ranged**” (not just nearest-neighbour interactions)

Interesting collective phenomena!

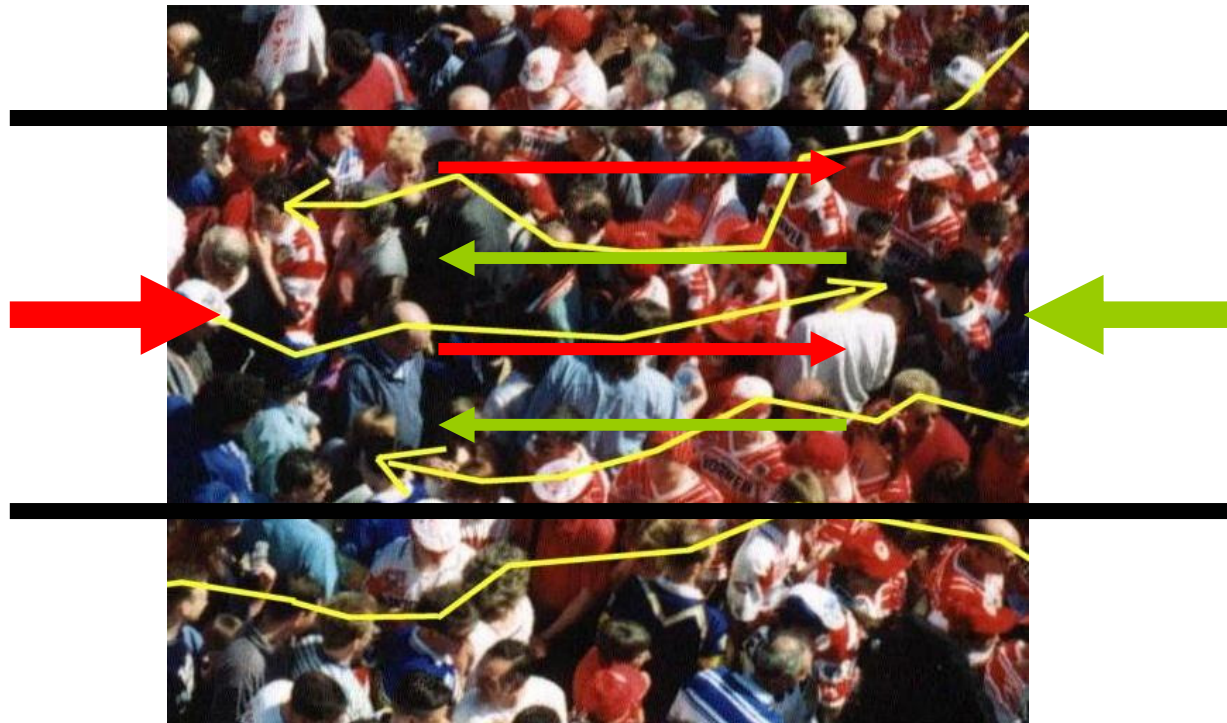
Collective Phenomena

jamming or clogging
(e.g. at exits)



no real challenge for modelling!

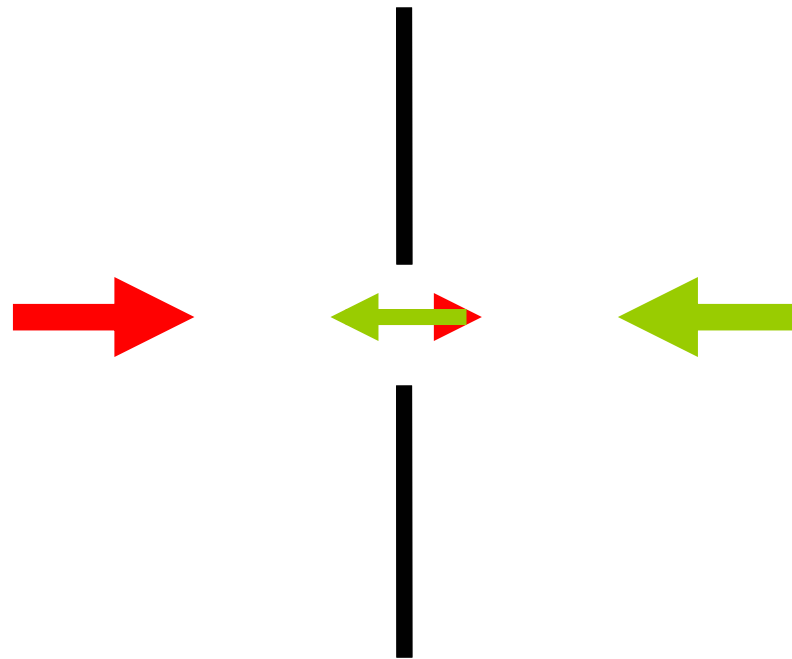
Lane Formation in Counterflow



Pedestrian motion



Oscillations of Flow Direction



Empirical Results

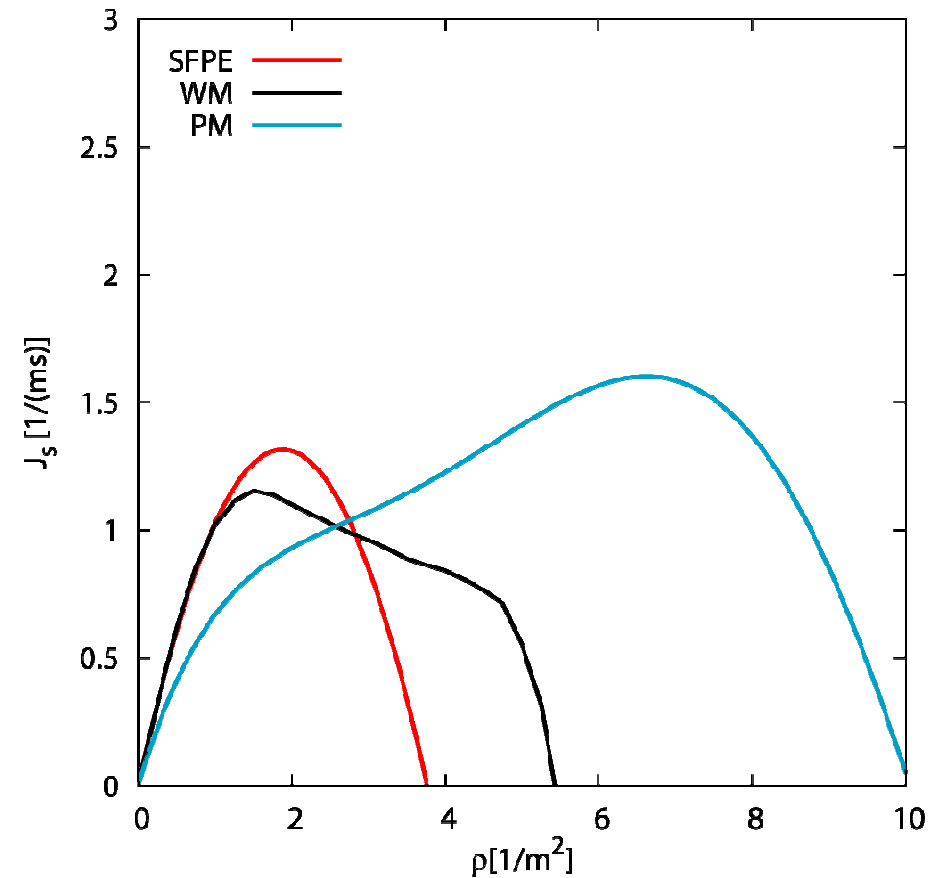
- not many quantitative results available
 - contradicting results (quantitative, sometimes even qualitative)
 - experiments not well documented
 - important for calibration of models
- Experiments with up to 250 soldiers
(in collaboration with FZ Jülich, University of Wuppertal)

Fundamental diagram

Specifications in guidelines

- Different shapes
- Capacity values C_s
 $C_s: 1.2 - 1.6 \text{ (ms)}^{-1}$
- Location of the maximum
 $\rho_C: 1.8 - 7 \text{ m}^{-2}$
- Location of ρ_0
 $\rho_0: 3.8 - 10 \text{ m}^{-2}$

Non-negligible differences
In particular for ρ_0



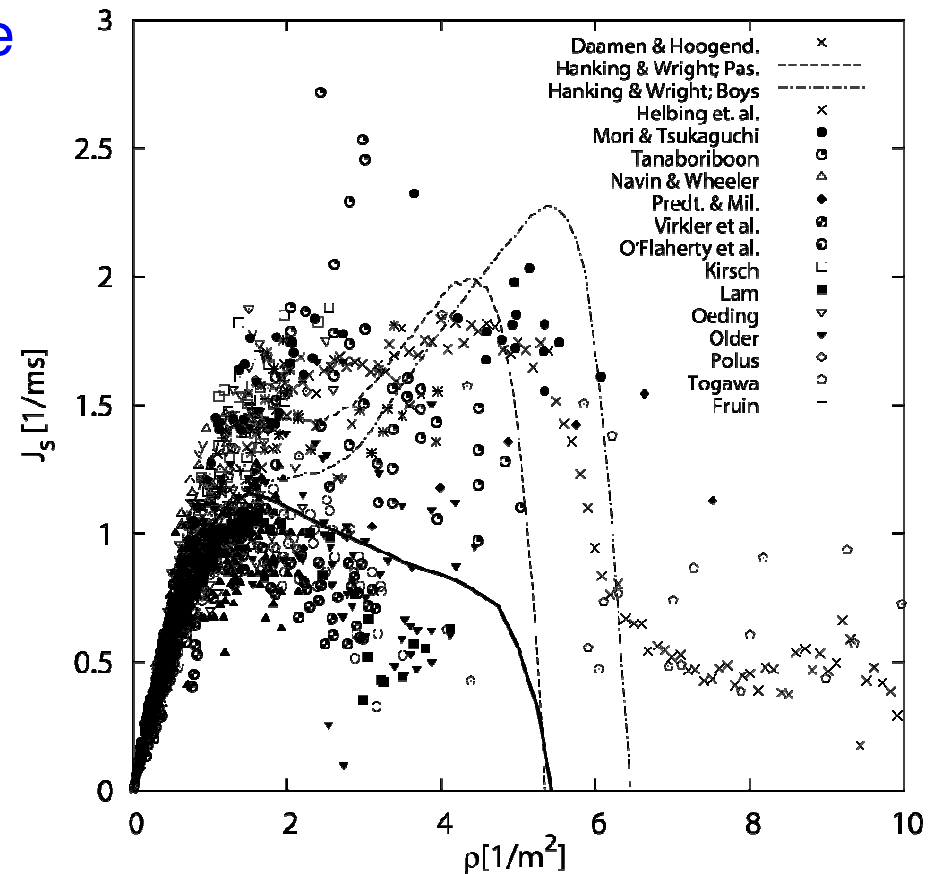
SFPE P. J. DiNenno (2002) *SFPE Handbook ...*
PM V. M. Predtechenskii and Milinskii (1978)
WM U. Weidmann (1993) *Transporttechnik ...*

Comparison of experimental data

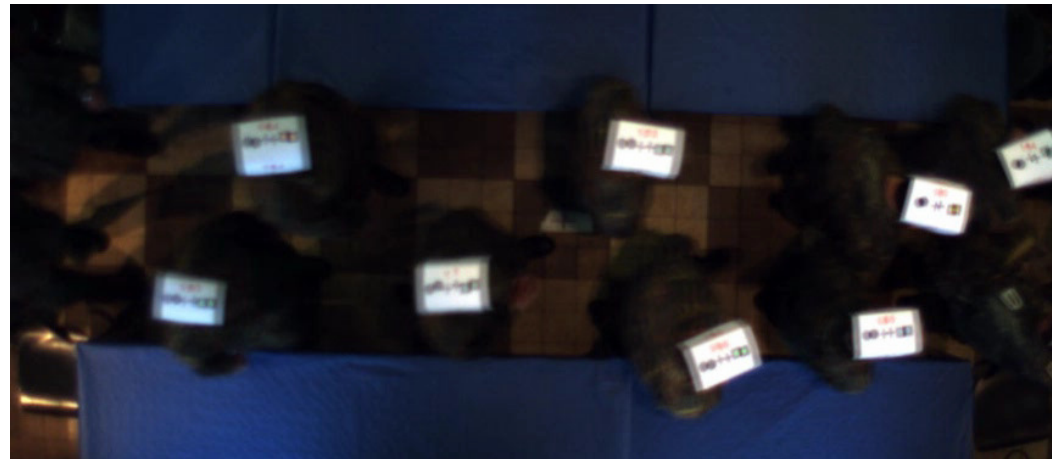
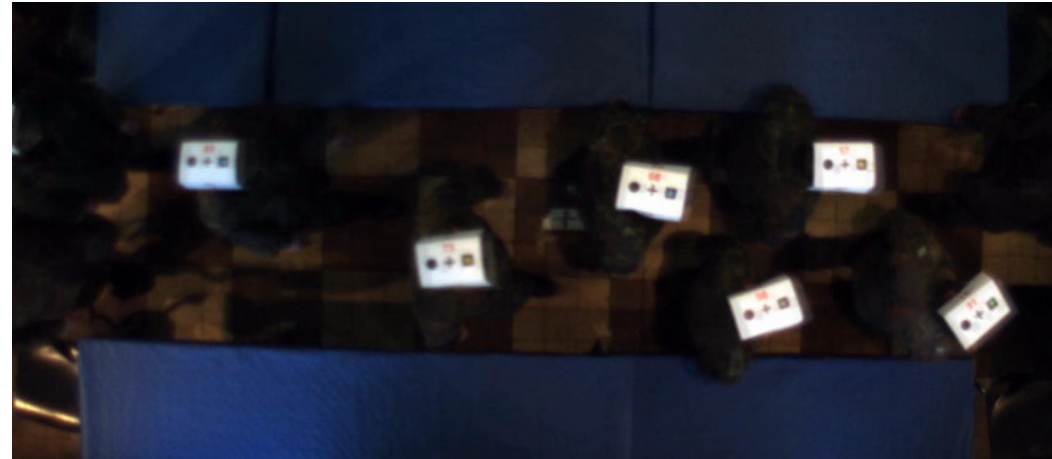
Causes discussed in the literature

- Uni- and bidirectional
- Way of measurement
- Fluctuations
- Culture and population demographics
- Psychological factors

Unfortunately most authors give not all necessary information!



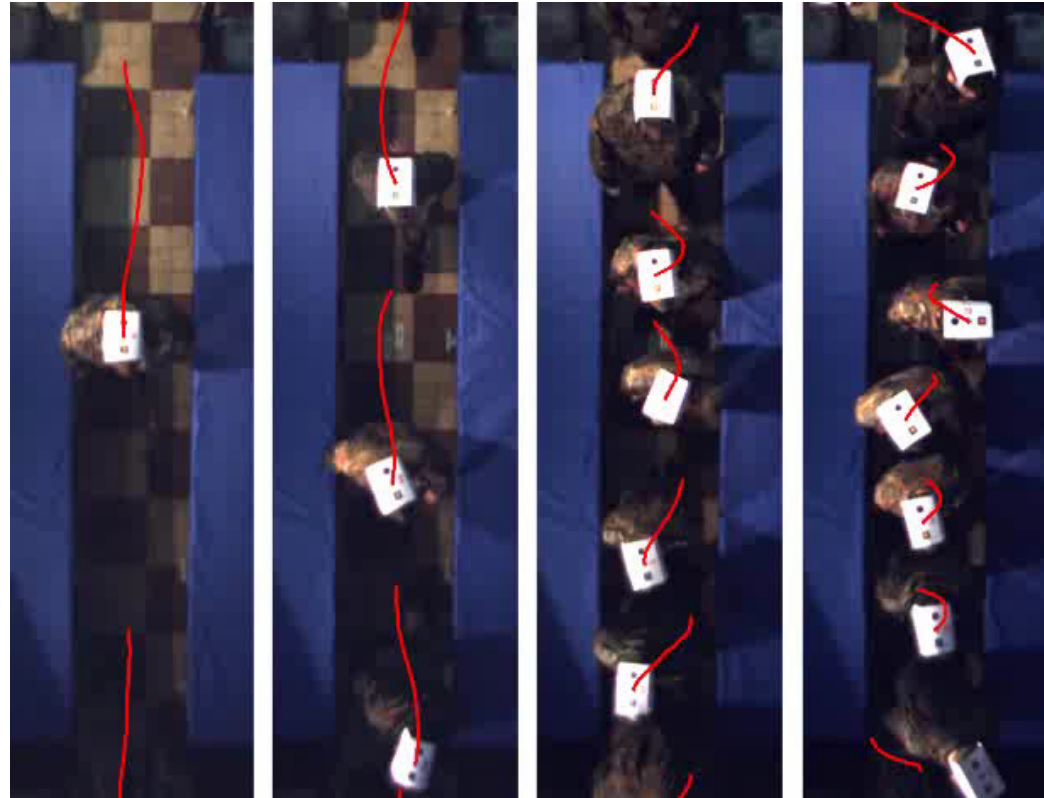
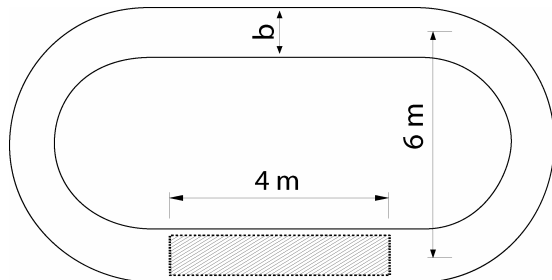
Flow vs. Density



Preliminary results

Fundamental diagram

- single file movement
- corridor width
 $b = 0.7\text{m}$
- unidirectional
- closed boundaries
- stationary states
- Number of pedestrians
 $N = 17 - 70$



$N=14$

$N=25$

$N=39$

$N=56$

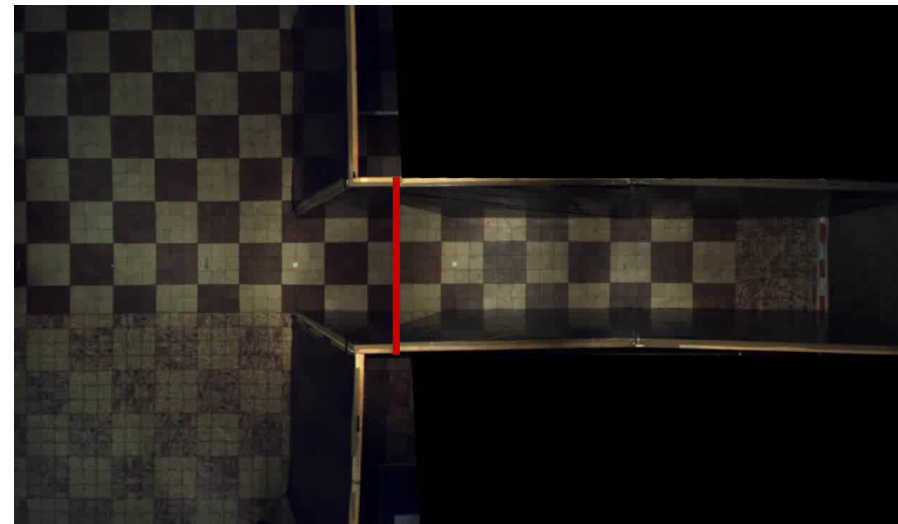
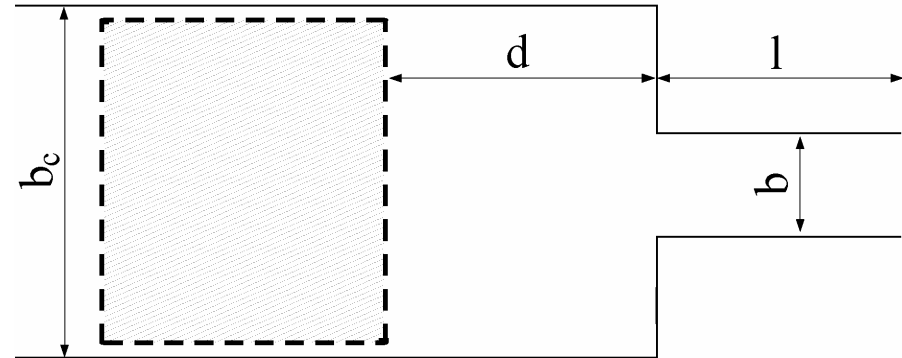
Bottleneck



Sets of the experiments: Part 2

Bottleneck flow

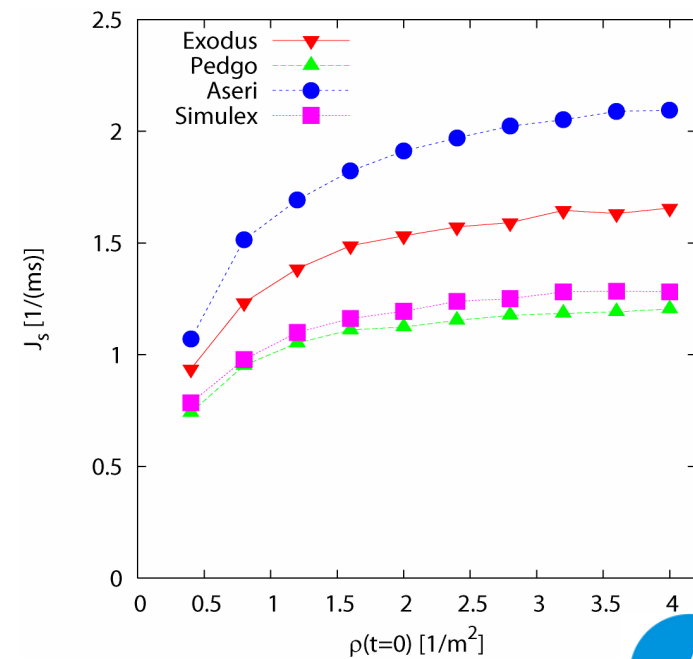
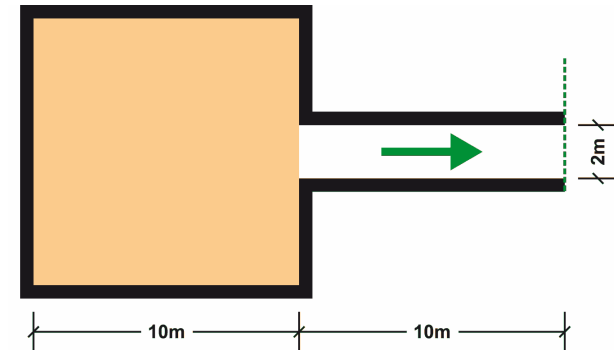
- Bottleneck width **b**
0.8, 0.9, ..., 2.5m
- Bottleneck length **l**
0.1, 2.0, 4.0m
- Corridor width **b_c**
4.0, 5.0, 6.0m
- Number of pedestrians **N**
50, 100, ..., 250
- Distance to the entrance **d**
1.0, 2.0, 3.0, 4.0m



Examples

Calculated egress times
(flow rates) of different
evacuation simulation tools
(Aseri, PedGO, Simulex and
BuildingExodus) will differ
significantly (factor 2 to 4)
(C. Rogsch, PED2005)

In particular for simple geometries



Chemotaxis

Ants can communicate on a chemical basis:

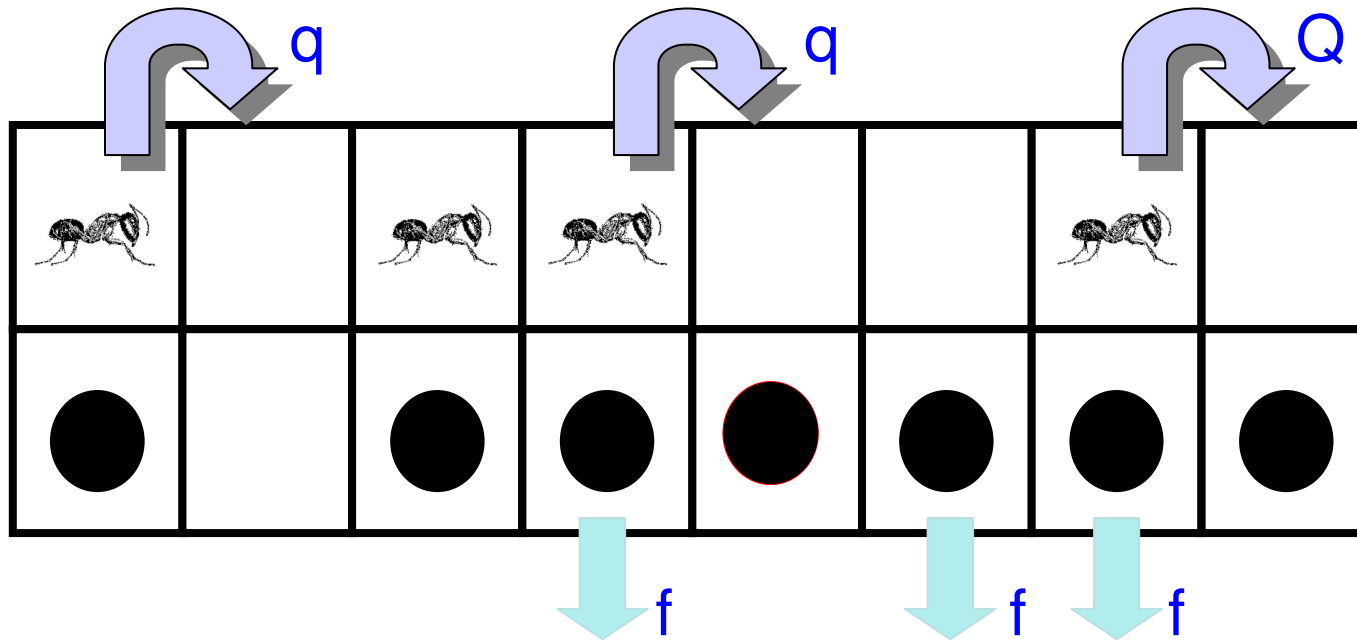
chemotaxis

Ants create a chemical trace of pheromones

trace can be “smelled” by other ants
follow trace to food source etc.

Ant trail model

- Dynamics:
1. motion of ants
 2. pheromone update (creation + evaporation)



parameters: $q < Q, f$

Pedestrian model

motion described by **stochastic** dynamics:

transition probabilities

reflects our lack of knowledge

works well for 'large' systems (← physics)

interactions:

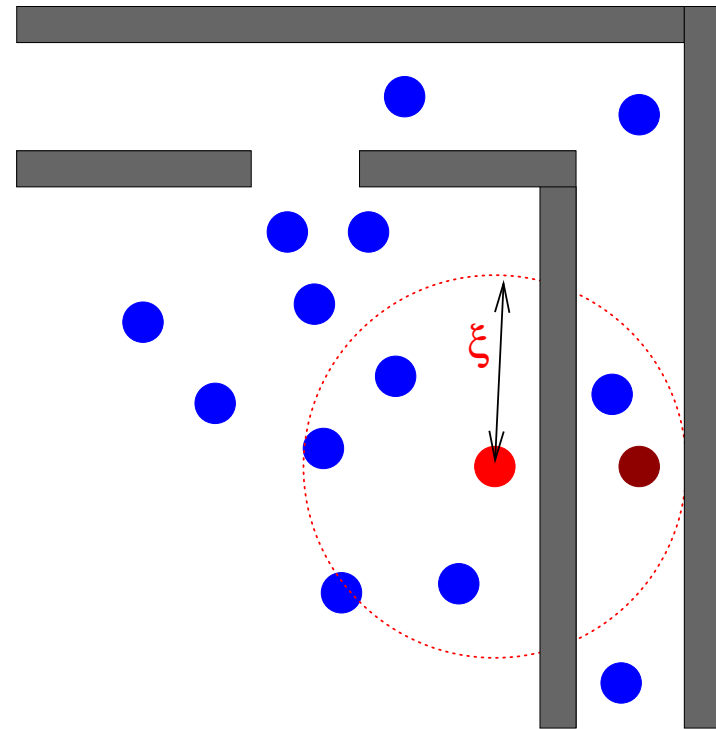
Virtual chemotaxis

chemical trace: *long-ranged* interactions are translated into *local* interactions with "*memory*"

Long-ranged Interactions

Problems for complex geometries:

Walls "screen" interactions



Models with **local** interactions ???

Floor Field CA: Basics

Cellular automaton model with stochastic dynamics

Space divided into cells (40*40 cm²)

Exclusion principle: no more than one pedestrian per cell

Discrete time: parallel (synchronous) dynamics

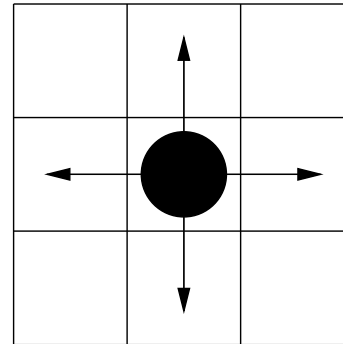
→ natural timescale

→ calibration and quantitative predications possible!!

Motion only to neighbour cells ($v_{\max} = 1$)

Transition Probabilities

Stochastic motion, defined by transition probabilities



0	$p_{-1,0}$	0
$p_{0,-1}$	$p_{0,0}$	$p_{0,1}$
0	$p_{1,0}$	0

3 contributions:

- Desired direction of motion
- Reaction to motion of other pedestrians
- Reaction to geometry (walls, exits etc.)

Unified description of these 3 components

Floor Field Model

Free motion: specified by average velocity $\langle \mathbf{v} \rangle$ and variance σ^2

Floor field = virtual field that modifies the transition probabilities

2 types:

- **Dynamic floor field:** is modified by the motion of the pedestrians (they create a “trace“)
- **Static floor field:** not influenced by pedestrians; determined by geometry

General principle: motion into direction of larger fields is preferred

Dynamic Floor Field

Motion increases field strength in starting cell

⇒ pedestrians change dynamic field

⇒ motion creates a **trace**

Dynamic floor field has dynamics:

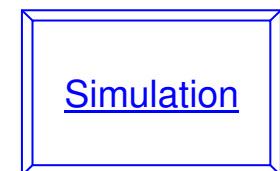
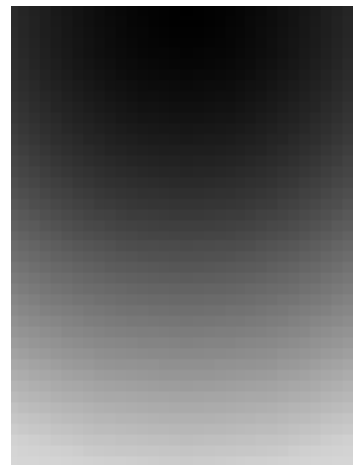
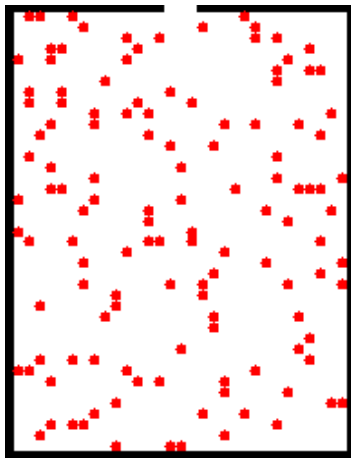
diffusion + **decay**

⇒ **broadening** and **dilution** of trace

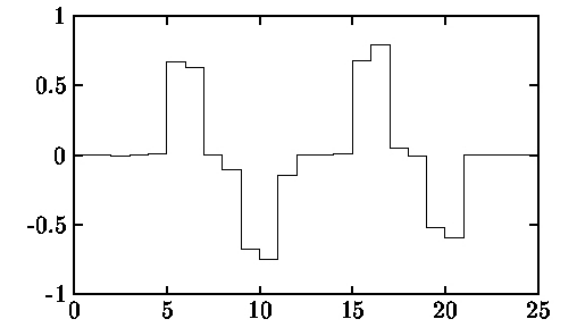
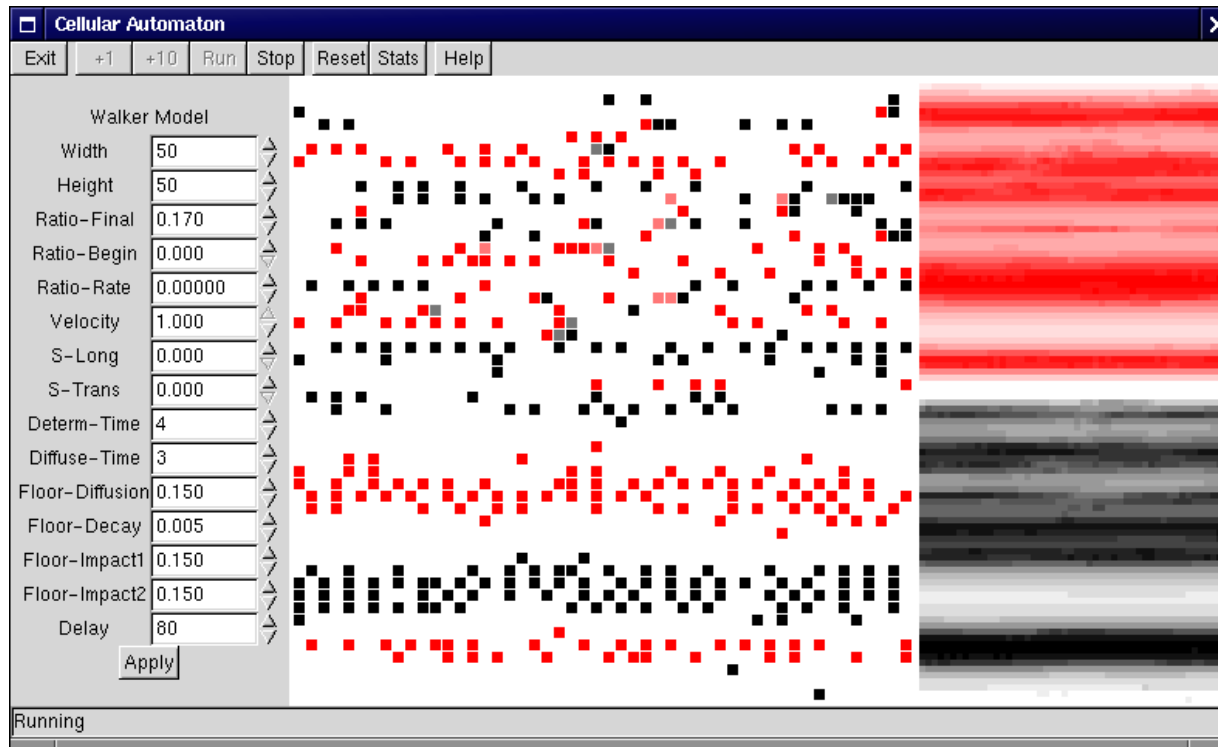
Static Floor Field

- Not influenced by pedestrians
- no dynamics (constant in time)
- modelling of influence of infrastructure

Example: Ballroom with one exit



Lane Formation



velocity profile

counterflow: left and right mover

Evacuation Simulations

Influence of the different floor fields:

individual behaviour (static) vs. **herding** (dynamic)

static field dominates: **normal situation**

full knowledge about infrastructure, e.g. shortest way to the exits

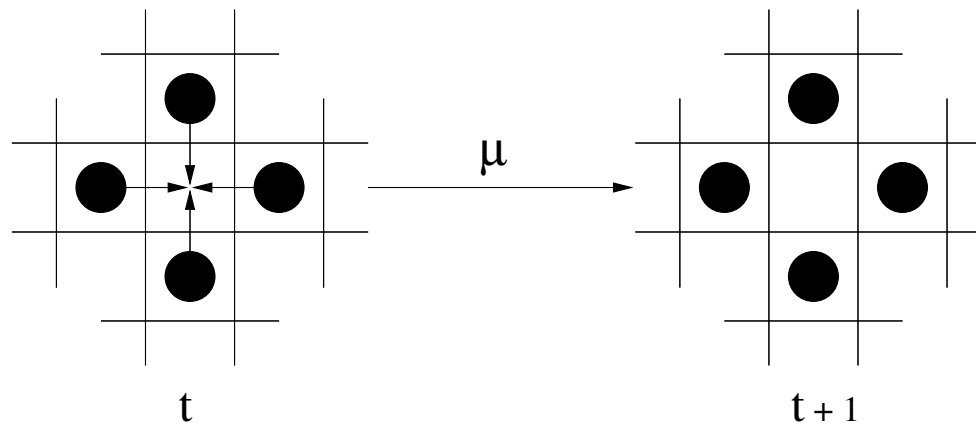
dynamic field dominates: **emergency situation** (“panic”)

herding behaviour

Friction

Conflict: 2 or more pedestrians choose the same target cell

Friction: not all conflicts are resolved!



friction constant μ = probability that no one moves

Artefact or Real Effect ?

conflicts reduce efficiency of simulations

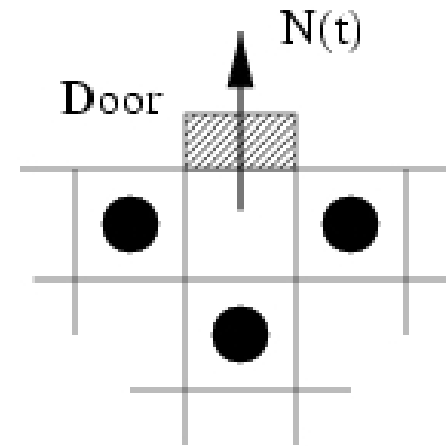
→ often avoided by special update choice

However: **Conflicts** and **friction** correspond to **real effects**, e.g.

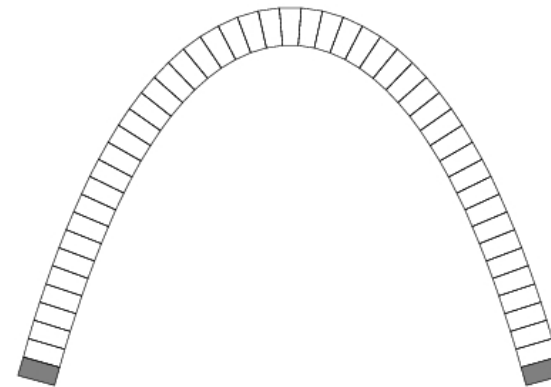
- physical contact
- moment of hesitation

Friction at Exits

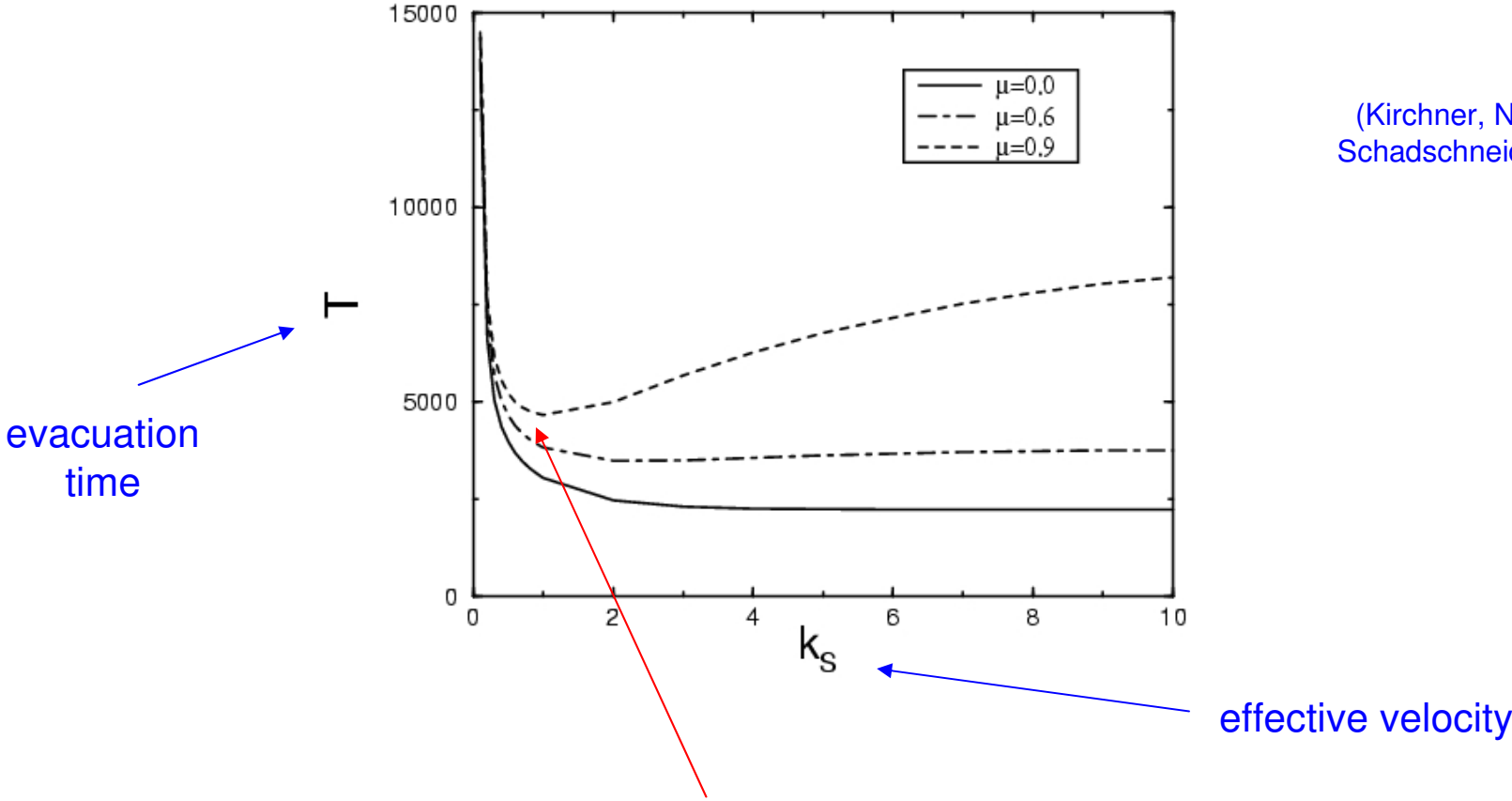
Friction at exits increases evacuation times by reducing the outflow



Granular materials:
Arching



Evacuation Scenario With Friction Effects



(Kirchner, Nishinari, Schadschneider 2003)

Faster-is-slower effect

Friction in Evacuation Processes

Friction most important close to exits and other bottlenecks
⇒ have a direct influence on evacuation times

away from exits it can even have positive effects, e.g.
because jamming at door is suppressed
⇒ Faster-is-slower effect

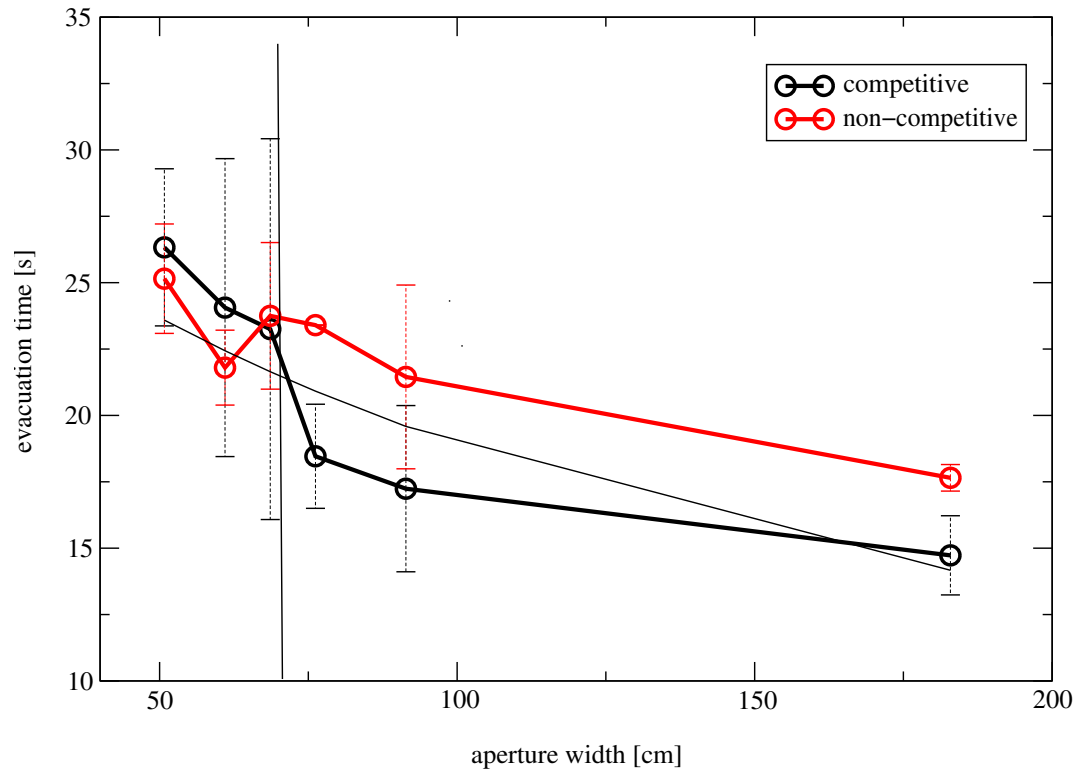
Competitive vs. Cooperative Behaviour

Experiment: egress from aircraft (Muir et al. 1996)

Evacuation times as function of 2 parameters:

- motivation level
 - competitive (T_{comp})
 - cooperative (T_{coop})
- exit width w

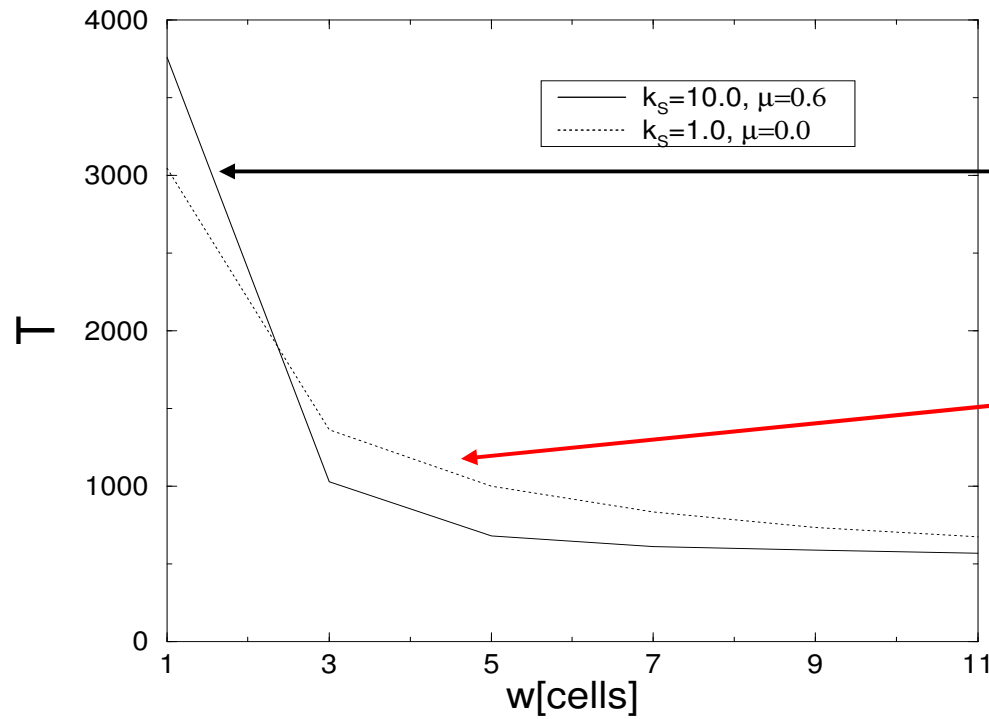
Empirical Egress Times



$T_{\text{comp}} > T_{\text{coop}}$ for $w < w_c$

$T_{\text{comp}} < T_{\text{coop}}$ for $w > w_c$

Model Approach



Competitive behaviour:
large k_S + large friction μ

Cooperative behaviour:
small k_S + no friction $\mu=0$

(Kirchner, Klüpfel, Nishinari,
Schadschneider, Schreckenberg 2003)

Fundamental diagram

empirically: non-symmetric

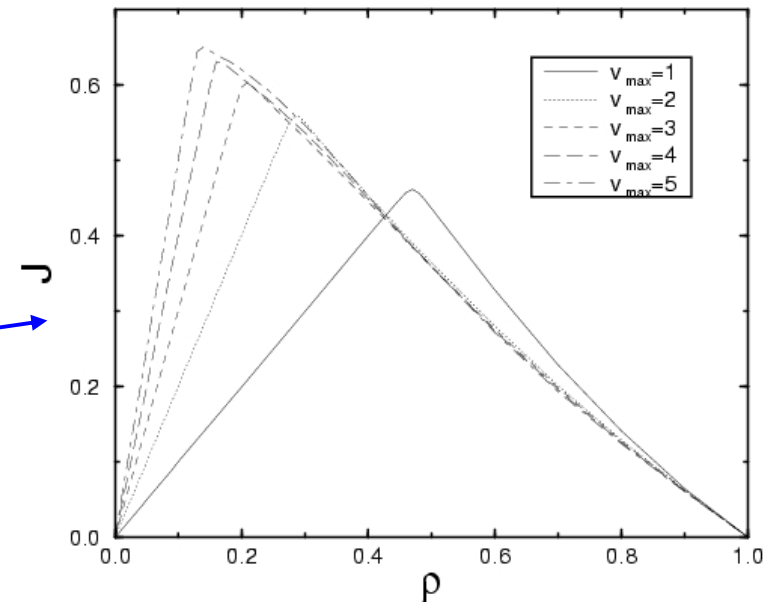
maximal flow at small densities

important: larger space
requirement at higher velocities

generalize model to $v_{\max} > 1$ →

asymmetric fundamental diagram

Dependence on maximal velocity



no non-monotonicity for realistic parameter values !

Summary

Ant traffic on existing trails and pedestrian dynamics can be described by similar models

interactions: local (real/virtual chemotaxis)

ant trails: anomalous fundamental diagrams possible
formation of loose clusters

pedestrian dynamics: no 'intelligence' required
collective effects reproduced (lane formation etc.)
applications to safety analysis