

# ERRATUM TO: ENTROPY OF HOMEOMORPHISMS ON UNIMODAL INVERSE LIMIT SPACES

H. BRUIN AND S. ŠTIMAC

If  $Q(x) = ax(1 - x)$  is a renormalisable quadratic map on the unit interval, say with non-trivial periodic interval  $J$  of period  $q$ , then the inverse limit space  $\varprojlim ([0, 1], Q)$  contains subcontinua  $G_i, 0 \leq i < q$ , that are homeomorphic to  $\varprojlim (J, Q^q)$  and are cyclically permuted by the shift-homeomorphism  $\sigma$ . In the proof of [1, Theorem 1.2], the step that a self-homeomorphism on  $\varprojlim ([0, 1], Q)$  can act isotopically to different powers of  $\sigma$  on different  $G_i$  ([1, p. 999]) is not justified. The existence of arc-components that are dense in the core inverse limit space  $\varprojlim ([c_2, c_1], Q)$  prevents this. Therefore, the large set of entropies mentioned in [1, Theorem 1.2] cannot be realised. Only if  $\varprojlim ([c_2, c_1], Q)$  is decomposable and the renormalisation is within the first period doubling cascade (and hence of period  $q = 2^n$ ), the above step holds, but this alone is too restrictive to lead to new values of the topological entropy. The correct statement is therefore the same as for the tent-family, i.e., it has the same form as [1, Theorem 1.1]:

**Theorem 0.1.** *Assume that  $Q$  is a quadratic map with positive topological entropy and  $\log s = h_{\text{top}}(Q)$ . If  $H$  is a homeomorphism on the inverse limit space  $\varprojlim ([0, 1], Q)$ , then the topological entropy  $h_{\text{top}}(H) = |R| \log s$ , where  $R \in \mathbb{Z}$  is such that  $H$  is isotopic to  $\sigma^R$ .*

This theorem can be proved in an analogous way as [1, Theorem 1.1], using the new result [2, Theorem 5.1], which says that every self-homeomorphism on the inverse limit space of a quadratic map  $Q$  with positive topological entropy is isotopic to  $\sigma^R$  for some  $R \in \mathbb{Z}$ , is given.

## REFERENCES

- [1] H. Bruin, S. Štimac, *Entropy of homeomorphisms on unimodal inverse limit spaces*, Nonlinearity **26** (2013), 991–1000.
- [2] H. Bruin, S. Štimac, *On isotopy of self-homeomorphisms of quadratic inverse limit spaces*, Preprint 2017. Arxiv....

Faculty of Mathematics, University of Vienna  
Oskar Morgensternplatz 1, 1090 Wien, Austria

`henk.bruin@univie.ac.at`

`http://www.mat.univie.ac.at/~bruin/`

Department of Mathematics, Faculty of Science, University of Zagreb

Bijenička 30, 10 000 Zagreb, Croatia

`sonja@math.hr`

`http://www.math.hr/~sonja`